

Physics of Stars

practice exam
Wednesday 8 June 2016, 13:00–15:00

Write clearly and be explicit in your answers, writing each step of your calculations.

- 1) The optical spectrum of a faint star indicates a spectral type of G2V and a geometric parallax measurement places it at a distance of 100 parsec. However, the star is observed to be 10 magnitudes fainter than expected. A sub-millimetre observation indicates the presence of an intervening, dark, spherical cloud of gas with a diameter of 100 AU, a temperature of 30 K and an opacity in the optical part of the spectrum of $k=0.002 \text{ cm}^2 \text{ g}^{-1}$ with no optical emissivity.
 - a) Assume a uniform density and calculate the density ρ of this cloud.
 - b) Assume a hydrogen mass fraction of $X=0.75$, a helium mass fraction of $Y=0.25$ and a negligible metallicity. Is this small cloud stable against collapse?
 - c) How much energy could be released to the surrounding interstellar medium if this cloud would fully collapse?
 - d) If 10% of the mass of this cloud would collapse onto a single central object, would a star be formed? If not, why not? If yes, what would be roughly the spectral type of the star once it has arrived on the Main-Sequence?
- 2) This question concerns atomic absorption lines in an optical spectrum.
 - a) Describe in words the formation process of an optically thin atomic line in the atmosphere of a star. Use the following key words: continuum, flux, opacity, core of the line, wings of the line, optical depth, geometric depth, temperature.
 - b) A weak line has a Gaussian shape with a Full Width Half Maximum of 2 \AA and a maximum depth of $1/\pi$ of the continuum flux. Calculate the equivalent width of this line.

Note the standard integral $\int_0^{\infty} e^{-ax^2} = \frac{1}{2} \sqrt{\pi/a}$
 - c) An absorption line is observed to be saturated. Make a clear sketch of the shape of this line in relation to the continuum flux in the spectrum. For clarity, describe the shape of this line in words.
- 3) This question deals with the energy production process in stars.
 - a) Explain why the proton-proton chains dominate the nuclear energy production in low-mass stars on the main sequence.
 - b) In the CNO-I cycle, the following nuclear reactions occur:
$$^{15}\text{O} \rightarrow ^{15}\text{N} + \dots$$
$$^1\text{H} + ^{15}\text{N} \rightarrow ^{12}\text{C} + \dots$$
Use the various conservation laws to argue which missing particles are created in these reactions.
 - c) Calculate how much total energy each of these reactions deliver to the stellar plasma.